

**Homework #3 (10 points) - Show all work on the following problems:**

*(Grading rubric: Solid attempt = 50% credit, Correct approach but errors = 75% credit, Correct original solution = 100% credit, Copy of online solutions = 0% credit)*

**Problem 1 (20 points):** Given a parallel plate capacitor immersed in sea water with permittivity  $\epsilon = 81\epsilon_0$ , permeability  $\mu = \mu_0$ , and resistivity  $\rho = 0.23 \Omega m$ , with a sinusoidally varying voltage  $V(t) = V_0 \cos(2\pi\nu t)$  with amplitude  $V_0$  and frequency  $\nu = 4 \times 10^8$  Hz between the plates, what is the ratio between the amplitudes of the conduction current and the displacement current  $\vec{J}_d = \frac{\partial \vec{D}}{\partial t}$ ?

**Problem 2 (30 points):** Calculate the total electromagnetic energy per unit time transported down a coaxial cable consisting of an inner cylinder with radius  $a$  and an outer cylinder with radius  $b$  (as in Example 7.13 in Griffiths). Assume the two conductors are held at a potential difference  $V$ , with current  $I$  flowing along the surface of the inner cylinder and back along the surface of the outer cylinder.

**Problem 3 (30 points):** Find the electromagnetic force between two equal point charges  $q$  separated by a distance  $2a$ , by integrating Maxwell's stress tensor over the plane equidistant between the two charges.

**Problem 4 (20 points):** A charged parallel-plate capacitor (two plates with area  $A$ , separated by distance  $d$ , carrying charge  $+Q$  and  $-Q$ ) has its positively charged plate in the  $x$ - $y$  plane ( $z=0$ ), and its negatively charged plate at  $z = d$ . There is thus a uniform electric field  $E$  pointing in the  $+z$  direction between the plates. In addition, there is a uniform external magnetic field  $B$  pointing in the  $+x$  direction.

**4a (10 points):** Find the magnitude and direction of the electromagnetic momentum in the space between the plates, in terms of  $E$ ,  $B$ ,  $A$ , and  $d$ .

**4b (10 points):** Now assume that a wire with resistance  $R$  is connected between the plates, along the  $z$ -axis, so that the capacitor slowly discharges. The current through the wire will experience a magnetic Lorentz force. What is the magnitude and direction of the total impulse (Impulse =  $\int \vec{F} dt$ ) delivered to the system by that force during the discharge, in terms of  $E$ ,  $B$ ,  $A$ , and  $d$ ?